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**MATHEMATICAL MODELING OF HIBRYD POWER SYSTEM BASE ON SPRING-GRAVITY GENERATOR, WIND FARM, SOLAR PANELS, MICRO HYDRO, AND POWER BANK AS A RENEWABLE SOURCE TO AVOID PLN ELECTRICITY THEFT**

By

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**Abstract:** *This paper constructs a mathematical model of power plant based on renewable energy sources including generators of spring-gravity, solar panels, wind turbine, micro hydro, power banks as energy storage, generator units and/or state electricity companies as an alternative source and the useful of photocell as efficiency control strategies, motion sensor for momentary lighting and or wi-fi switches in response to fluctuating demand loads. By combining various types of environmentally friendly power plats, it is hoped that they can accommodate fluctuations in load demant and electricity sources produced in such a way that optimal conditions are accieved, and reability with control parametrization enhancing technique as dynamic switching control methode in response to fluctuating demand loads. Furthermore, with the abundance of renewable energy sources in order to avoid PLN electricity theft.*

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**INTRODUCTION**

Along with population growth and today's developments, the need for electricity today has increased to become a very vital need in the wheel of life, not only in big cities but in remote villages, plantation areas or small islands-even in dire need of electricity. The strategy of the generator unit system in procuring electricity sources for electrification has been widely known. However, to maintain a consistent energy supply in this way, it turns out that a lot of the energy produced is wasted when the load that must be met decreases. Unfortunately the generator unit system is not able to store the remaining electrical energy so that a lot of electrical energy is wasted, especially when the output from the generator exceeds the demand load. Operating the genset unit at a low power level for an extended period of time can result in scaling of the engine block cylinder of the generator set. These conditions

require special treatment and will cost a higher treatment than regular treatment. The benefits of having electricity facilities include lighting, entertainment, communication, information, industry, irrigation, transportation, security, safety, defense and or research support facilities.

One alternative to procuring an efficient power source for electrification with relatively low operating costs is the design of a wind, solar and micro hydro-based hybrid system with an operational strategy of controlling efficiency using photocell, motion sensor and or wifi android os. The system is used to procure a power source that has the ability to store the remaining electrical energy and the ability to switch when the load to be fulfilled fluctuates up or down. Therefore, to accommodate the procurement of efficient and renewable or environmentally friendly electricity sources together, from the applied side it is very interesting and challenging to study the development of a mathematical model of a hybrid system of electrical energy based on wind, solar and micro hydro as alternative energy for electrification, at the same time. with the conditions of the pandemic situation, the use of photocell, motion sensor and or wifi android os for efficiency control is very relevant to be applied as an attitude to maintain health protocols.

## 2. Battery Model

An important aspect that has been developed is to carry out dynamic modeling of battery recharge and discharge, namely by taking the following approach: for example  $C(t)$  is the battery capacity at time  $t$ , measured in watt-hour units. The battery dynamic model is given as follow:

$$\dot{C}(t) = R(t) + D(t)$$

where  $R(t)$  = recharge rate and  $D(t)$  = discharge rate. For example,  $P_B(t)$  is the net energy available for the battery, with the understanding that  $P_B(t) > 0$  means the recharge cycle is in progress and  $P_B(t) < 0$  is the discharge cycle is in progress.

The recharge rate is given by the following model:

$$R(t) = \begin{cases} \frac{K_1 P_B(t)}{K_1 + C(t)}, & \text{jika } P_B(t) \geq 0, \\ 0, & \text{jika } P_B(t) < 0. \end{cases}$$

Where  $K_2$  is a risk factor, operational in the field the value of  $K_2$  1.4 which means that only about 70% of the energy stored in the battery can be used to supply the system load. Note that  $K_1$  and  $K_2$  are assumed to use lead-acid batteries. Since the battery is considered as part of the system,  $P_B(t)$  becomes a function that depends on other system components and the system load, in this case how much windmill dynamo capacity is used and how much lamp load is used so as to achieve efficient system operational costs. So far the battery model has not affected the conversion from DC to AC (and vice versa).

## 3. Hybrid System Power Generation Configuration

All In general, the hybrid system power plant (HSPP) configuration has components as described in the previous section [1, 2, 3, 5, 6, 7, 12], plus renewable sources of energy, such as windmill generators or micro-hydro power plants. In the HSPP-Parallel Topology configuration, the inverter and the rectifier can be combined into one, which is a two-way inverter (a bi-direction inverter). Thus this configuration is more efficient, because the AC generator can directly supply the demand load without losing energy due to going through

the inverter first first. In this work we focus only on the HSPP-parallel topology configuration as shown in Figure 3.1

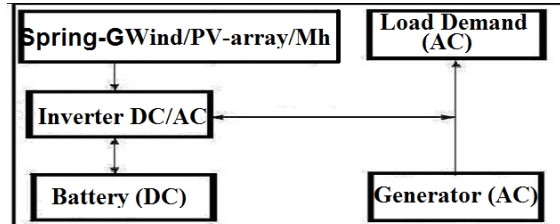


Figure 3.1

The capacity of the windmill dynamo and battery is smaller or larger than the values listed in the table can be calculated. The windmill and battery dynamo system is very useful for lighting plantation areas or remote areas that are far from a power source or where the State Electricity Company (PLN) electricity network has not been installed.

furthermore, with the abundance of renewable energy sources in order to avoid PLN electricity theft.

Approximation of power or capacity of each component of the windmill dynamo system and battery by providing maximum power and life is listed in the table. The electricity supply for remote areas needs to be developed in a sustainable manner with a touch of science and technology that is environmentally friendly. Renewable energy sources (solar, wind, water flow, gravity, ...) will be a potential source to be utilized so that it can produce electrical energy.

Table Approximation of the system unit capacity of the battery and windmill dynamo (12 Volts)

Battery Ampere	Maximum Battery Capacity	Maximum Windmill Dynamo Capacity
6 Ampere	72 Watt-hour	7 Watt- hour
10	120 Watt-hour	12 Watt- hour
20	240 Watt- hour	24 Watt- hour
60	720 Watt- hour	72 Watt- hour

The energy produced by the windmill dynamo during the day can be used directly to serve the demand load or stored in batteries, and the energy stored in the battery can be used for lighting at night. The following is a table of correspondence for the use of lamp load capacity (in Watts) and battery capacity so that it can be lit for 12 hours for lighting at night.

Table Approximate battery capacity and lamp power capacity (12 Volts) for 12 hours

Battery Ampere	Maximum Battery Capacity	Maximum Lamp Power Capacity/Load
6 Ampere	72 Watt-hour	6 Watt
10 Ampere	120 Watt-hour	10 Watt
20 Ampere	240 Watt-hour	20 Watt
60 Ampere	720 Watt-hour	60 Watt

#### 4. Solar Radiation Model

K Sunlight as a renewable renewable energy source is one of the energy sources currently in Indonesia that really needs to be developed, given the increasing demand for electrical energy, this is in line with the increasingly limited energy sources from fossil fuels. One of the sources of energy from sunlight is used to generate electricity. Therefore, electricity procurement for remote areas or in urban areas needs to be developed in a sustainable manner with a touch of science and technology that is environmentally friendly.

The next step is to record data every certain time interval of the voltage generated by the solar panels. In this research, data is taken or data is recorded on an electric voltage meter every 1 minute from 07.06 to 17.34 Jakarta time zone on 10 October. Plot the data obtained by the measuring instrument at Cartesian coordinates using Microsoft Excel software which is shown in the following graph

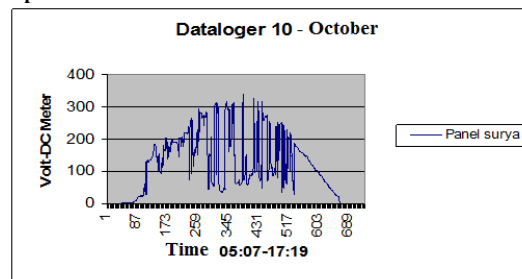


Figure 4.1 Plot of sun intensity data from sunrise–sunset obtained on October-10.

For data that fluctuates, it is very difficult to make a mathematical model, therefore for the operation of a hybrid system, data from day to day must be interpolated as an external input to the system and the mathematical model obtained applies to large amounts of data (data collected from year to year), or normal shape. However, there is data that is collected in just a day if it is plotted it will produce a graph that is close to the normal curve. This happened because it was a sunny day and the sunlight produced normal power, as shown in the following figure:

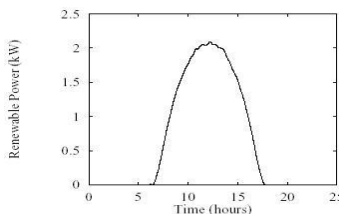


Figure 4.2 Plot of solar intensity data that forms a normal curve.

The solar intensity power profile (clear weather) from the datalogger which is close to the normal curve is taken as a mathematical model because this condition shows the maximum solar power output. The resulting normal curve is used as a mathematical model for the intensity of the sun from sunrise to sunset. Mathematical modeling of the curve as a function of solar panel power is

$$P_p = P_{max}/108 [ (t-6)^3 - 4(t-9)^3 + 6(t-12)^3 - 4(t-15)^3 + (t-18)^3 ]$$
 Where  $P_p(t)$  is the amount of power generated by the solar panel at  $t$ ,  $t$  is the time from sunrise to sunset and  $P_{max}$  is the maximum power of the solar panel. The function or model is a normal model obtained from data on sunny weather conditions, sunlight hitting the solar panel from sunrise to sunset.

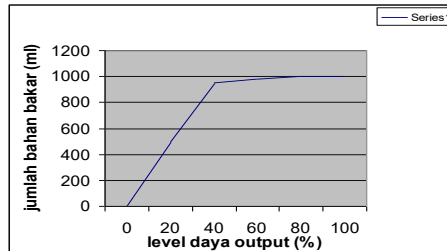
### 5. Genset Fuel Consumption Model

First of all the generator is off or at an output level of 0% of maximum capacity, this condition is a condition where the generator does not operate. By installing a transparent measuring tube in the fuel tank, the amount of fuel used will be measured. Furthermore, after the generator is ready to operate, install the output power level of 20% of its maximum capacity, by shifting the direction of the needle on the generator engine. For 1 hour the generator is turned on at that level, the amount of fuel used can be measured by observing the measuring tube that has been installed, at that output level the generator can spend about 500 ml of fuel, with energy released 10 kw, at this level the amount of fuel consumed expended relatively little, according to the energy produced.

The approximate power or output capacity of the generator with the amount of fuel every 1 hour is given in the following table:

Power	Amount of fuel (ml)
0 % (off)	0
20 %	500
40 %	950
60 %	980
80 %	1000
100 %	1000

Table 5.1 Power level data with the amount of fuel used every 1 hour. Furthermore, the data obtained, plotted using Microsoft excel software and obtained the following graph:



And the graph is transformed into a cost function graph, which is obtained as follows:

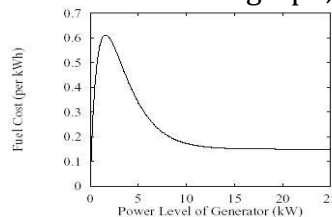


Figure 5.1 Graph of the relationship between generator power levels and fuel prices.

The following models obtained from existing data.

$g_1(x) = 2((0,2x + 0,5)0,4 - (0,5)0,4)e^{-0,1x} + 0.15(1 - e^{-0,1x})$ . Where  $x$  is the generator power level (kw), and  $g_1(x)$  is the fuel cost.

### 6. Hybrid System Power Plant Operational Strategy

There are many ways to operate a hybrid system as described in [1, 8, 9, 10]. In order for the operational cost of the hybrid system to be efficient, an optimization study is needed to obtain a strategic solution for the operation of the system. Optimization studies need to be carried out because they will provide an accurate solution in designing and operating a

hybrid system, so as to achieve the most efficient operational costs. In this study, build a dynamic system model such that the overall operational costs of the system are efficient:

1. If the demand load is less than or equal to the power generated by the generator, the inverter will continue the remaining energy from the generator, windmill or solar panels to charge the battery.
2. If the demand load is less than or equal to the power generated from the combined generator set, windmill and solar panels, but the demand load is greater than the power generated by the generator set, then some of the energy from the turbine and solar panels is used to meet the demand load while the rest is used to charge battery.
3. If the demand load exceeds the power generated from the combined generator, windmill and solar panels, then the battery together with other units supply energy to meet the demand load.

From the steps described above, the operational mathematical model of PLSH so that the overall operational costs of the system are efficient are as follows:

For example,  $P_B(t)$  is the net electrical energy in the battery,  $PP(t)$  is the energy produced by solar panels,  $PK(t)$  is the energy produced by the windmill,  $PG(t)$  is the energy produced by the generator and  $PL(t)$  is the demand load. Furthermore, the three operating options above can be modeled mathematically as follows:

$$P_B(t) = \begin{cases} (P_p(t) + P_k(t) + P_g(t) - P_L(t))K_3, & \text{jika } P_g(t) \geq P_L(t), \\ K_3(P_p(t) + P_k(t) + P_g(t) - P_L(t)), & \text{jika } P_g(t) + K_3(P_p(t) + P_k(t)) \geq P_L(t), \\ P_p(t) + P_k(t) - \frac{P_L(t) - P_g(t)}{K_3}, & \text{jika } P_g(t) + K_3(P_p(t) + P_k(t)) < P_L(t), \end{cases}$$

where  $K_3$  is the inverter efficiency constant.

$P_B(t)$  positive

$$\text{If } P_L(t) > P_g(t) + K_3(P_p(t) + P_k(t))$$

and  $P_B(t)$  negative

$$\text{If } P_L(t) > P_g(t) + K_3(P_p(t) + P_k(t))$$

with the dynamic model of the system, namely dynamic recharge and discharge of batteries, no energy is wasted. Next, combining the  $P_B(t)$  expression with the dynamic charge of the battery, we get a dynamic model of the whole hybrid system, namely:

$$\dot{C}(t) = \begin{cases} \frac{K_1 K_3 (P_p(t) + P_k(t) + P_g(t) - P_L(t))}{K_1 + C(t)}, & \text{jika } P_g(t) \geq P_L(t), \\ \frac{K_1 (K_3 (P_p(t) + P_k(t) + P_g(t) - P_L(t)))}{K_1 + C(t)}, & \text{jika } P_g(t) + K_3 (P_p(t) + P_k(t)) \geq P_L(t) \\ K_2 \left( P_p(t) + P_k(t) - \frac{(P_L(t) - P_g(t))}{K_3} \right), & \text{jika } P_g(t) + K_3 (P_p(t) + P_k(t)) < P_L(t) \end{cases}$$

In practice the generator can be operated at one of a limited number of output levels, for numerical simulation, the generator control function is assumed that the generator can be operated at an output level of 0% (off), 40% (low), 60% (medium), 80% (high) and 100% (maximum) of the maximum capacity. The proposed objective function consists of three cost factors. Mathematically, it can be modeled as follows:

1. Generator operational costs are given by model

$$\int_0^{t_f} P_G(t)g_1(P_G(t))dt$$

with

$P_G(t)$  = level output generator in  $t$ ,

$$0 \leq P_G(t) \in \{0\%, 40\%, 60\%, 80\%, 100\%\} \leq T_{max}$$

$g_1(P_G(t))$  = generator fuel cost efficiency function at time  $t$ ,

$$g_1(x) = 2((0.2x + 0.5)^{0.4} - (0.5)^{0.4})e^{-0.1x} + 0.15(1 - e^{-0.1x}).$$

2. Charges for recharge and discharge of batteries are given by model

$$\int_0^{t_f} (C(t) - K)^2 dt$$

with

$C(t)$  = battery capacity at the time  $t$ ,

$K$  = constant, keep the battery capacity 80% of the maximum capacity,

3. Cost of generator fines for not operating at short time intervals given the model:

$$\int_0^{t_f} g_2 dt, g_2(x) = ((x + 0.01)^{0.25} - (0.01)^{0.25}) e^{-5x}$$

## 7. Numerical Results and Discussion

Some examples of case studies are shown with a 24-hour demand load profile as shown in Figure 7.1 "LOAD". Battery capacity is limited between  $C_{min} = 20$  kWh and  $C_{max} = 100$  kWh. Several  $C_o$  and  $C_t$  conditions are given for simulation:

Case 1:  $C_o = 80$  and  $C_t = 80$ . Figure 7.2 shows the optimal charging level, generator level and operating time.

Case 2:  $C_o = 95$  and  $C_t = 80$ . Figure 7.3 shows the optimal charging level, generator level and operating time.

Case 3: In this case it is set that the generator does not operate from midnight to 4 am. In practice, this generator operating time limit is very common in the community for reasons of environmental friendliness from noise for communities close to the generator location. Given  $C_o = 90$  and  $C_t = 80$ . Figure 7.4 shows the optimal charging level, generator level and operating time.

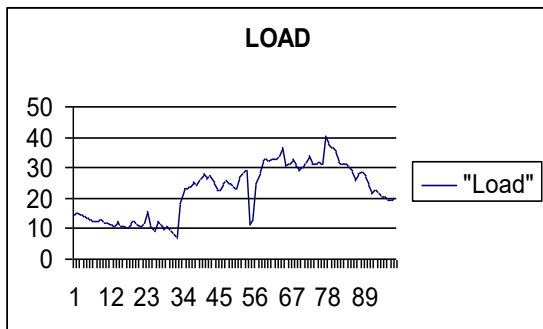


Figure 7.1 "LOAD"

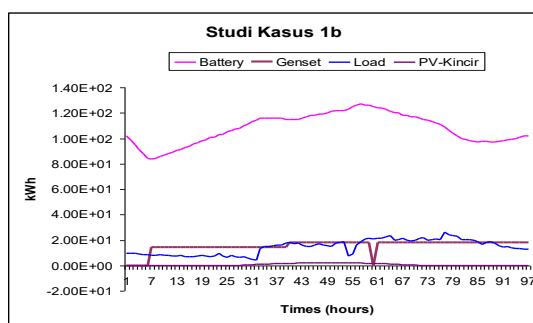


Figure 7.2 "Case 1"

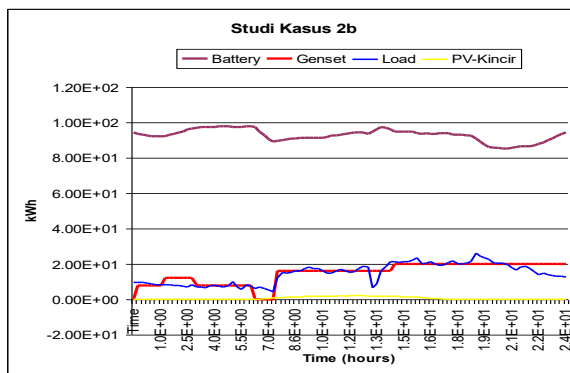


Figure 7.3 "Case 2"

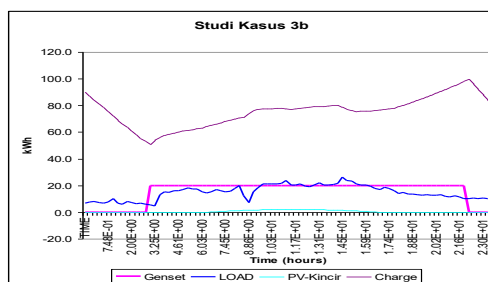


Figure 7.4 "Case 3"

## CONCLUSION

In this paper, we have modelled and developed control strategy for a electricity hybrid systems base on renewable sources using photocell, motion sensor and or wifi switch. Numerical results of the simulation model were presented. The profile recharge and discharge dynamics of lead acid battery as battery bank have shown. The strategy of using photocells, motion sensors and or wifi switch is very relevant in the situation of the pandemic, post-covid-19 pandemic and the era of the US-Iran war energy crisis. The control strategy policies obtained from this model can aid in the future design of better adaptive control strategies.

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